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AN INTERACTIVE COMPUTER PROGRAM FOR SIZING SPACECRAFT MOMENTUM STORAGE DEVICES

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F. J. Wilcox, Jr.

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National Aeronautics and Space Administration

Langley Research Center Hampton, Virginia 23665

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AN INTERACTIVE COMPUTER PROGRAM FOR SIZING SPACECRAFT MOMENTUM STORAGE DEVICES

Floyd J. Wilcox, Jr. Langley Research Center

SUMMARY

An interactive computer program has been developed which computes the sizing requirements for nongimbled reaction wheels, control moment gyros (CMG), and dual momentum control devices (DMCD) used in Earth-orbiting spacecraft. The program accepts as inputs the spacecraft's environmental disturbance torques, rotational inertias, maneuver rates, and orbital data. From these inputs, wheel weights are calculated for a range of radii and rotational speeds. The shape of the momentum wheel may be chosen to be either a hoop, solid cylinder, or annular cylinder. The program provides graphic output illustrating the trade-off potential between the weight, radius, and wheel speed. A number of the intermediate calculations such as the X-, Y-, and Z-axis total momentum, the momentum absorption requirements for reaction wheels, CMG's, DMCD's, and basic orbit analysis information are also provided as program output.

INTRODUCTION

Earth-orbiting spacecraft utilize nongimbled reaction wheels, control moment gyros (CMG), and dual momentum control devices (DMCD) for momentum storage and control, and the development of accurate momentum wheel sizing requirements is essential for effective spacecraft design. As part of the Langley Research Center's Computer-Aided Spacecraft Design effort, an interactive computer program has been developed to size momentum wheels. The program accepts as input the spacecraft's environmental disturbance torques, rotational inertias, maneuver rates, vehicular orientation, and orbital data. Momentum wheel weights are calculated for a range of wheel radii and rotational speeds, and are provided as graphical output to illustrate the trade-off potential between the weight, radius, and wheel speed. Intermediate calculations such as the X-, Y-, and Z-axis total momentum, the momentum absorption requirements for reaction wheels, CMG's, DMCD's, and basic orbit analysis information are also provided as output.

The momentum wheel sizing computer program listing is given in the appendix.

PROGRAM DESCRIPTION

The momentum wheel sizing computer program provides an interactive graphics technique for determining the wheel size and weight for various momentum storage

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and control devices on Earth-orbiting spacecraft. The program is written in ANSI standard FORTRAN on a Control Data Corporation (CDC) CYBER 173 computer. The graphics output is generated using Tektronix Plot 10 software routines in conjunction with a Tektronix 4014/15 graphic terminal. The program should be easily adapted to and can be executed on any host computer with this graphics package and remote terminal.

A simplified flow diagram of the momentum wheel sizing program is shown in figure 1.

Inputs and Assumptions

The user provides the following inputs: spacecraft environmental disturbance torques, rotational inertias, maneuver rates, orbit altitudes and inclination, vehicle orientation, and celestial orientation. These inputs are provided as outputs from two other Langley Research Center Computer-Aided Spacecraft Design programs, (1) the Spacecraft Design and Cost Model (SDCM), reference 1, and (2) the Large Area Space System (LASS), reference 2. The orbital equations of motion were obtained from reference 3. The relationship between the orbital reference frames and the vehicle reference frames is shown in figure 2. The input parameters are:

INOSE - Vehicle Pointing Orientation

- 1. Sideways
- 2. Nose Down
- 3. Nose Forward

ISATOR - Celestial Orientation

- 1. Earth
- 2. Solar
- 3. Inertial

XNNN - Number of Gimbled Configurations for CMG

- A Apoapsis Altitude
- P Periapsis Altitude

ORBINC - Orbit Inclination

TL - Number of Orbits Between Wheel Unloading

TACCEL - Maneuver Acceleration Time

PDOTR
$$\begin{pmatrix} X \\ Y \\ Z \end{pmatrix}$$
 - X-, Y-, Z-Axis Spacecraft Maneuver Rate

UPSILN - Angular Pivoting for DMCD

TA
$$\begin{pmatrix} X \\ Y \\ Z \end{pmatrix}$$
 - X-, Y-, Z-Axis Atmospheric Disturbance Torque

TG
$$\begin{pmatrix} X \\ Y \\ Z \end{pmatrix}$$
 - X-, Y-, Z-Axis Gravity Gradient Disturbance Torque

TS
$$\begin{pmatrix} X \\ Y \\ Z \end{pmatrix}$$
 - X-, Y-, Z-Axis Solar Disturbance Torque

$$\begin{pmatrix} X \\ Y \\ Z \end{pmatrix}$$
 J - X-, Y-, Z-Axis Spacecraft Rotational Inertia

A major assumption of the program is that the X-axis is the spin axis while the Y- and Z-axes are transverse. Also, the spacecraft's orbit may be either circular or elliptical. Although all the momentum control wheels are normally the same size, the X-, Y-, and Z-axes momentum absorption requirements are not identical, therefore, it is necessary to determine the wheel weight for the axis with the largest momentum absorption requirement.

Orbit Analysis

The first step of the orbit analysis portion of the program is to analyze the ellipse representing the orbit, as shown in figure 3.

From the figure, the semimajor axis, a, is calculated by

$$a = \frac{(2R + A + P)}{2}$$

The radius at periapsis, RP, is calculated by

$$RP = R + P$$

the focus of the ellipse, c, is calculated by

$$c = a - RP$$

and the eccentricity, e, is calculated by

$$e = \frac{c}{a}$$

where R is the radius of the Earth.

In the case of a circular orbit, the semimajor axis becomes the circle's radius which is also the radius at periapsis.

$$a = RP$$

This forces both the focus and eccentricity to zero

$$c = 0$$

$$e = 0$$

The orbital period, T, is then calculated using Kepler's 3/2 Law

$$T = \frac{2a^{3/2}}{\sqrt{u}}$$

where u is Earth's gravitational constant.

The mean orbital motion, N, is calculated using

$$N = \sqrt{\frac{u}{a^3}}$$

and the eccentric anomaly, E, by

$$E = N + e \sin (N) + \frac{1}{2} e^2 \sin (2N)$$

In the case of a circular orbit, the last two terms of the preceding equation are forced to zero and the eccentric anomaly becomes

$$E = N$$

Using the above calculations, the maximum orbital angular rate of change, $\dot{\theta}$, which is at perigee, is determined from

$$\dot{\theta} = \frac{N\sqrt{1 - e^2}}{\left[1 - e \cos(E)\right]^2}$$

For a circular orbit, the maximum rate of change is the mean orbital motion such that

$$\dot{\theta} = N$$

Total Momentum

To calculate the total momentum in each of the three spacecraft's body axes, three different momentums are taken into account: (1) maneuver momentum, (2) environmental disturbance torque momentum, and (3) orientation tracking momentum.

The maneuver momentums, HXMAN, HYMAN, and HZMAN, in all three axes are calculated using the following equations:

$$HXMAN = \frac{XJ(PDOTRX)}{57.3}$$

$$HYMAN = \frac{YJ(PDOTRY)}{57.3}$$

$$HZMAN = \frac{ZJ(PDOTRZ)}{57.3}$$

To compute the disturbance torque momentum, the total disturbance torques, XDT, YDT, and ZDT, are first calculated by summing the atmospheric, solar, and gravity gradient torques by

$$XDT = TAX + TSX + TGX$$

$$YDT = TAY + TSY + TGY$$

$$ZDT = TAZ + TSZ + TGZ$$

Using these totals, the disturbance torques, HTX, HTY, and HTZ, are then computed using

HTX = XDT (TL)(T)

HTY = YDT (TL)(T)

HTZ = ZDT (TL)(T)

To compute the orientation tracking momentums, HTRAKX, HTRAKY, and HTRAKZ, the program first determines whether the spacecraft is solar oriented, inertial oriented, or Earth oriented. If the spacecraft is either solar or inertially oriented, there is no orientation tracking momentum and the following assignments are made:

HTRAKX = 0.0

HTRAKY = 0.0

HTRAKZ = 0.0

If the spacecraft is Earth oriented, the program will determine whether its body axis is sideways, nose down, or nose forward with respect to the orbital velocity vector (fig. 2). The following assignments are made if its body axis is

HTRAKZ = 0.0

(3) Nose forward: HTRAKZ = 0.0 HTRAKY = YJ($\dot{\theta}$) HTRAKZ = 0.0

The total momentum in each axis is computed by summing the maneuver, disturbance torque, and orientation tracking momentums

HX = HXMAN + HTX + HTRAKX

HY = HYMAN + HTY + HTRAKY

HZ = HZMAN + HTZ + HTRAKZ

Control Device's Momentum Absorption Requirements

The momentum absorption requirements for the reaction wheel, CMG, and DMCD are calculated to determine the wheel weight. The maximum momentum in any axis, HMAX, is used for the calculation of nongimbled reaction wheel weight. Using an intrinsic FORTRAN function, HMAX is determined by

HMAX = AMAX1 (HX, HY, HZ)

Here HMAX will be assigned the largest value between HX, HY, and HZ. To compute the CMG momentum for computing wheel weight, the minimum momentum in any axis, HMIN, is first calculated using another intrinsic FORTRAN function

HMIN = AMINI (HX, HY, HZ)

Here HMIN will be assigned the smallest value between HX, HY, and HZ. From this, the CMG slew angle, GAMMA, is calculated from

$$GAMMA = TAN^{-1} \left[\frac{(XNNN-2) \ HMIN}{(XNNN) \ HMAX} \right]$$

Then using the preceding HMIN and GAMMA calculations, the CMG wheel momentum, HCMG, is calculated using

$$HCMG = \frac{HMIN}{(XNNN) \sin (GAMMA)}$$

The peak gimble rate, DELDOT, is computed by

$$DELDOT = \frac{HCMG}{57.3 \text{ (TACCEL)}}$$

and the peak torquer torque, TCMG, by

$$TCMG = \frac{(HCMG) AMAX1 (PDOTRX, PDOTRY, PDOTRZ)}{57.3}$$

To compute the DMCD momentum for computing wheel weight, the spin and transverse axis momentum absorption requirements must be calculated. The DMCD configuration for both the spin and transverse axes is shown in figure 4.

The spin axis absorption momentum, DELTHU, is calculated by

$$DELTHU = \frac{HX}{2}$$

and the transverse axis absorption momentum by

$$HU = \frac{AMAX1 (HY, HZ)}{2(\frac{UPSILN}{2})}$$

From these calculations, the total DMCD wheel momentum, HTDMCD, is computed by summing the spin and transverse axes absorption momentums

HTDMCD = DELTHU + HU

Wheel Weight

The final step of the program is to calculate the wheel weight. The wheel mass is calculated from the relationship between the rotational inertia of the wheel and its radius,

$$I = MR^2$$

Since the angular momentum, L, is equal to the rotational inertia of the wheel, I, multiplied by its angular velocity (wheel speed),

 $L = I\omega$

Then

$$L = MR^2 \omega$$

and

$$M = \frac{L}{R^2 \omega}$$

For a solid cylinder:

$$I = \frac{MR^2}{2}$$

and

$$L = \frac{MR^2}{2} \omega$$

and

$$M = \frac{2L}{R^2 \omega}$$

Finally, for an annular cylinder

$$I = M \frac{\left(R_1^2 + R_2^2\right)}{2}$$

and

$$L = M \frac{\left(R_1^2 + R_2^2\right)\omega}{2}$$

and

$$M = \frac{2L}{\omega(R_1^2 + R_2^2)}$$

where R_1 is the wheel's inner radius and R_2 is the outer radius. The acceleration of gravity, ACC, at the spacecraft's altitude is then calculated by

$$ACC = \frac{u}{RP^2}$$

The wheel masses are next multiplied by the acceleration of gravity to determine the wheel weight at the spacecraft's altitude. Thus, the equations used in computing wheel weight are

(1) For a hoop
$$W = \frac{L \text{ (ACC)}}{R^2 \omega}$$

(2) For a solid cylinder
$$W = \frac{2L \text{ (ACC)}}{R^2 \omega}$$

(3) For an annular cylinder
$$W = \frac{2L \text{ (ACC)}}{\omega \left(R_1^2 + R_2^2\right)}$$

Trade-Off and Output

Calculated wheel weight curves are shown in figures 5 through 7 for wheel radii varying from 1 inch (2.54 cm) to 10 inches (25.4 cm) and wheel speeds of 500 to 5000 rpm's in increments of 500 rpm's to illustrate the trade-off potential between weight, radius, and wheel speed. Weights of hoop, solid cylinder, and annular cylinder momentum wheels are presented for the nongimbled, CMG and DMCD systems. Calculations were made in U.S. Customary Units. Conversion factors for values used in this report are given in table 1. The program's input default values, which were used to generate the weight curves (figs. 5 to 7), are given in figure 8.

In addition to the weight curves, values of 22 calculated parameters are outputted, including the maximum torque in any axis which is calculated by

$$TMAX = \frac{AMAX1 (HXMAN, HYMAN, HZMAN)}{TACCEL + AMAX1 (XDT, YDT, ZDT)}$$

These other calculated parameters are

RP - Radius at periapsis

 $\dot{\theta}$ - Maximum orbital rate of change

T - Orbital period

$$H = \begin{pmatrix} X \\ Y \\ Z \end{pmatrix} MAN - X-, Y-, Z-axis maneuver momentum$$

HT
$$\begin{pmatrix} X \\ Y \\ Z \end{pmatrix}$$
 - X-, Y-, Z-axis disturbance torque momentum

HTRAK $\begin{pmatrix} X \\ Y \\ Z \end{pmatrix}$ - X-, Y-, Z-axis orientation tracking momentum

$$H \left\{ \begin{array}{c} X \\ Y \\ Z \end{array} \right\}$$
 - X-, Y-, Z-axis total momentum

HMAX - Maximum momentum, any axis

HCMG - CMG wheel momentum

HTDMCD - DMCD wheel momentum

DELDOT - Peak gimble rate

TCMG - Peak torquer torque

TMAX - Maximum torque in any axis

Calculated values of the output parameters are given in figure 9 for the weight curves illustrated.

CONCLUDING REMARKS

An interactive computer program has been developed at the Langley Research Center to size momentum wheels for various momentum storage and control devices for orbiting spacecraft. The program considers hoop, solid cylinder, and annular cylinder wheels.

Wheel weights are calculated and are shown for a series of wheel radii and wheel rotational speeds. Intermediate calculated parameters are also presented.

MOMENTUM WHEEL SIZING PROGRAM

The momentum wheel sizing program listing is given in this appendix.

```
PROGRAM WHEEL (INPUT, OUTPUT, TAPE1, TAPE2, TAPE3)
      REAL N
      COMMON INPUT, LOC, REAL, EXP
      COMMON /WEIR/ WEIGH1, WEIGH2, WEIGH3, WEIGH4, WEIGH5,
     *WEIGH6, WEIGH7, WEIGH8, WEIGH9, WEIGHO, R
      COMMON /URPI/U,RP,PI
      DIMENSION R(122), WEIGH1(122), WEIGH2(122)
      DIMENSION WEIGH3(122), WEIGH4(122), WEIGH5(122)
      DIMENSION WEIGH6(122), WEIGH7(122), WEIGH8(122)
      DIMENSION WEIGH9(122), WEIGHO(122)
       DIMENSION LOC(5), REAL(9), EXP(12), INPUT(277)
          RADIUS OF EARTH
C
       DATA RE/3441.66/
          EARTH'S GRAVITATIONAL CONSTANT
C
       DATA U/1.407850464E16/
       DATA PI/3.141592654/
       DATA WEIGH1(1), WEIGH2(1), WEIGH3(1), WEIGH4(1), WEIGH5(1),
      *WEIGH6(1), WEIGH7(1), WEIGH8(1), WEIGH9(1), WEIGH0(1),
      *R(1)/11*101./
       CALL INITT(120)
       CALL FEET(RE)
       PRINT *,"ENTER 1 FOR DEFAULT VALUES"
PRINT *,"ENTER 2 FOR VALUES FROM LAST RUN"
20
       PRINT *,
       PRINT *, "ENTER 3 FOR PERMANENTLY SAVED VALUES"
       PRINT *, "ENTER 4 TO STOP"
       READ *, IVALUE
       PRINT 5025
       IF (IVALUE.EQ.1) GOTO 40
       IF (IVALUE.EQ.2) GOTO 60 IF (IVALUE.EQ.3) GOTO 70
       IF (IVALUE.EQ.4) GOTO 999
       GOTO 20
       READ (1,5000) (LOC(J),J=1,3)
READ (1,5005) (REAL(J),J=1,9)
40
       READ (1,5010) (EXP(J),J=1,12)
       READ (1,5015) (INPUT(J),J=1,277)
       REWIND 1
       CALL REPLACE
       GOTO 80
       READ (2,5000) (LOC(J),J=1,3)
READ (2,5005) (REAL(J),J=1,9)
60
        READ (2,5010) (EXP(J),J=1,12)
        READ (2,5015) (INPUT(J),J=1,277)
        REWIND 2
```

```
CALL REPLACE
       GOTO 80
       READ (3,5000) (LOC(J),J=1,3)
70
       READ (3,5005) (REAL(J), J=1,9)
       READ (3,5010) (EXP(J),J=1,12)
READ (3,5015) (INPUT(J),J=1,277)
       REWIND 3
       CALL REPLACE
       INOSE = LOC(1)
80
       ISATOR= LOC(2)
       XMM = LOC(3)
       APOA= REAL(1)
       PER= REAL(2)
        ORBINC= REAL(3)
        TL = REAL(4)
        TACCEL= REAL(5)
        PDOTRX= REAL(6)
        PDOTRY= REAL(7)
        PUOTRZ= REAL(8)
        UPSILN= REAL(9)
        TAX = EXP(1)
        TGX = EXP(2)
        TSX = EXP(3)
        TAY = EXP(4)
        TGY = EXP(5)
        TSY = EXP(6)
        TAZ = EXP(7)
        TGZ = EXP(8)
        TSZ = EXP(9)
        XJ = EXP(10)
        YJ = EXP(11)
        ZJ= EXP(12)
WRITE (2,5000) (LOC(J),J=1,3)
WRITE (2,5005) (REAL(J),J=1,9)
        WRITE (2,5010) (EXP(J), J=1,12)
        WRITE (2,5015) (INPUT(J),J=1,277)
        REWIND 2
        PRINT *,"DO YOU WANT TO SAVE NEW VALUES PERMANENTLY?"
PRINT *,"ENTER 1 FOR YES"
PRINT *,"ENTER 2 FOR NO"
        READ *,JOE
        PRINT 5040
         IF (JOE.EQ.1) 90,95
         WRITE (3,5000) (LOC(J),J=1,3)
 90
         WRITE (3,5005) (REAL(J),J=1,9)
         WRITE (3,5010) (EXP(J),J=1,12)
         WRITE (3,5015) (INPUT(J),J=1,277)
         REWIND 3
         CALL FEET (APOA)
 95
         CALL FEET(PER)
```

```
COMPUTE SEMIMAJOR AXIS OF ELIPSE
  C
        A = (2.*RE+APO\Lambda+PER)*0.5
            COMPUTE ORBITAL PERIOD
  C
        T = 2.*PI*A**(1.5)/SQRT(U)
            COMPUTE RADIUS OF PERIAPSIS
  C
        RP= RE+PER
            COMPUTE FOCUS OF ELIPSE
  C
        C= A-RP
            COMPUTE ECCENTRICITY
  C
        ECC = C/A
            COMPUTE MEAN ORBITAL MOTION
  C
        N = SORT(U/A**3)
           COMPUTE ECCENTRIC ANOMALLY
  C
        E= N+ECC*SIN(N)+0.5*ECC**2*SIN(2*N)
            COMPUTE MAX ORBITAL ANGULAR RATE
  C
        THETAD= (N*SQRT(1.-ECC**2))/((1.-ECC*COS(E))**2)
            COMPUTE MOMENTUM REQUIREMENTS FOR SIZING NON-GIMBALLED
   C
            MOMONTUM WHEELS
   C
             MANEUVER MOMENTUM
   C
         HXMAN= XJ*PDOTRX/57.3
         HYMAN= YJ*PDOTRY/57.3
         HZMAN= ZJ*PDOTRZ/57.3
             COMPUTE DISTURBANCE TORQUES
   C
         XDT= TAX+TGX+TSX
         YDT= TAY+TGY+TSY
         ZDT= TAZ+TGZ+TSZ
             COMPUTE DISTURBANCE TORQUE MOMENTUM
   C
         HTX= XDT*TL*T
         HTY= YDT*TL*T
         HTZ= ZDT*TL*T
             COMPUTE ORIENTATION TRACKING MOMENTUM REQUIREMENTS
   C
         GOTO (120,100,100) ISATOR
             INERTIAL AND SOLAR ORIENTATION
   C
         HTRAKX= 0.0
   100
         HTRAKY = 0.0
         HTRAKZ= 0.0
         GOTO 200
             EARTH ORIENATION
   C
         GOTO (140,160,180) INOSE
   120
              SIDEWAYS
   C
         HTRAKX= XJ*THETAD
    140
         HTRAKY= 0.0
         HTRAKZ= 0.0
          GOTO 200
              NOSE DOWN
    C
          HTRAKX= 0.0
    160
          HTRAKY= YJ*THETAD
          HTRAKZ= 0.0
          GOTO 200
              NOSE FORWARD
____ C
```

```
180
      HTRAKX= 0.0
      HTRAKY= YJ*THETAD
      HTRAKZ= 0.0
           COMPUTE TOTAL MOMENTUM PER ORBIT
C
200
      HX= (HXMAN+HTX+HTRAKX)
      HY= (HYMAN+HTY+HTRAKY)
      HZ= (HZMAN+HTZ+HTRAKZ)
           COMPUTE MAX MOMENTUM ANY AXIS
C
      HMAX = AMAXI(HX, HY, HZ)
C
           COMPUTE MAX TORQUE ANY AXIS
      TMAX= AMAX1 (HXMAN, HYMAN, HZMAN)/TACCEL+AMAX1 (XDT, YDT, ZDT)
          COMPUTE MINIMUM MOMENTUM
C
      HMIN= AMINI(HX,HY,HZ)
          COMPUTE SKEW ANGLE
C
      GAMMA= ATAN((XNNN-2.)*HMIN/(XNNN*HMAX))
          COMPUTE CMG WHEEL MOMENTUM
C
      HCMG= HMIN/(XNNN*SIN(GAMMA))
C
          COMPUTE PEAK GIMBLE RATE
       DELDOT= HCMG/TACCEL*57.3
          COMPUTE PEAK TORQUER TORQUE
C
       TCMG= HCMG*AMAX1(PDOTRX,PDOTRY,PDOTRZ)/57.3
          COMPUTE SPIN AXIS ABSORPTION REQUIREMENT
C
       DELTHU= HX/2.
          COMPUTE TRANSVERSE AXIS ABSORPTION REQUIREMENT
C
       HU= AMAX1(HY,HZ)/(2.*UPSILN/57.3)
          COMPUTE TOTAL DISCO WHEEL MOMENTUM
C
       HTDMCD= DELTHU+HU
       PRINT 5030,(IMPUT(J),J=163,167),APOA
PRINT 5030,(IMPUT(J),J=168,172),RP
       PRINT 5030, (INPUT(J), J=173,177), THETAD
       PRINT 5030, (INPUT(J), J=178, 182), T
       PRINT 5025
       PRINT 5035, (INPUT(J), J=273,277)
       PRINT 5025
       PRINT 5030, (INPUT(J), J=183, 187), HXMAN
       PRINT 5030, (INPUT(J), J=188, 192), HYMAN
       PRINT 5030, (INPUT(J), J=193, 197), HZMAN
       PRINT 5025
       PRINT 5030, (INPUT(J), J=198, 202), HTX
       PRINT 5030,(INPUT(J),J=203,207),HTY
       PRINT 5030, (INPUT(J), J=208,2]2), HTZ
       PRINT 5025
       PRINT 5030, (INPUT(J), J=213,217), HTRAKX
       PRINT 5030, (INPUT(J), J=218, 222), HTRAKY
       PRINT 5030, (INPUT(J), J=223, 227), HTRAKZ
       PRINT 5025
       PRINT 5030, (INPUT(J), J=228,232), HX
       PRINT 5030, (INPUT(J), J=233, 237), HY
       PRINT 5030, (INPUT(J), J=238,242), HZ
       PRINT 5025
```

```
PRINT 5030, (INPUT(J), J=243,247), HMAX
      PRINT 5030, (INPUT(J), J=248, 252), TMAX
      PRINT 5030, (INPUT(J), J=253,257), HCMG
      PRINT 5025
      PRINT 5030, (INPUT(J), J=258, 262), DELDOT
      PRINT 5030, (INPUT(J), J=263,267), TCMG
      PRINT 5030, (INPUT(J), J=268,272), HTDMCD
      PRINT 5040
      REWIND 3
      PRINT *,"DO YOU WANT WHEEL SPEED, SIZE AND WEIGHT PLOT?"
PRINT *,"ENTER 1 FOR NON-GIMBLED PLOT"
220
      PRINT *, "ENTER 2 FOR CMG PLOT"
      PRINT *, "ENTER 3 FOR DMCD PLOT"
      PRINT *, "ENTER 4 FOR NO PLOT"
      READ *, IPLOT
      IF (IPLOT.LT.1.OR.IPLOT.GT.4) GOTO 220
      GOTO (240,260,280,20) IPLOT
      CALL STUFF (HMAX, 1)
240
       GOTO 220
      CALL STUFF (HCMG, 2)
260
      GOTO 220
280
       CALL STUFF (HTDMCD, 3)
       GOTO 220
       CALL FINITT(0,700)
999
      FORMAT (515)
5000
      FORMAT (5F10.3)
5005
5010
      FORMAT (5E10.4)
      FORMAT (9(4A10,A5/),9(5A10/),12(6A10/),23(5A10/))
5015
      FORMAT (5F5.2)
5020
      FORMAT (1X)
5025
      FORMAT (5A10,E14.7)
5030
      FORMAT (6A10)
5035
      FORMAT (///)
5040
       STOP
       END
C
          SUBROUTINE USED TO CHANGE PLOT AXES VALUES
C
C
       SUBROUTINE CHANGE(XVALUE, YVALUE, XMIN, XMAX, YMIN, YMX, JJ)
       INTEGER XVALUE, YVALUE
       PRINT *,"DO YOU WANT NEW GRAPH?"
PRINT *,"IF YES ENTER 1"
PRINT *,"IF NO ENTER 2"
5
       READ *,JJ
       IF (JJ.EQ.1) 20,10
IF (JJ.EQ.2) 120,5
10
       PRINT *, "DO YOU WANT TO CHANGE AXIS MAX AND MIN VALUES"
20
       PRINT *,"IF YES ENTER 1"
       PRINT *, "IF NO ENTER 2"
       READ *,II
```

```
IF (II.EQ.1) 40,80
                PRINT *, "ENTER X-AXIS MIN AND MAX VALUE"
40
                READ *,XMIN,XMAX
                IF (XMIN.EQ.O.O.OR.XMIN.GE.XMAX) GOTO 40
                IF (XMIN.NE.1.0.OR.XMAX.NE.10.0) JJ=1
                PRINT *, "ENTER Y-AXIS MIN AND MAX VALUE"
60
                READ *, YMIN, YMAX
                IF (YMIN.GE.YMAX) GOTO 60
                PRINT *,"DO YOU HANT TO CHANGE # OF INTERVALS"
80
                PRINT *,"IF YES ENTER 1"
                PRINT *,"IF NO ENTER 2"
                READ *,KK
                 IF (KK.EQ.1) 100,120
                PRINT *, "ENTER # OF X-AXIS INTERVALS"
 100
                 READ *,XVALUE
                 PRINT *, "ENTER # OF Y-AXIS INTERVALS"
                READ *,YVALUE
 120
                 RETURN
                 END
 C
                          SUBROUTINE USED TO PLOT CURVES
 C
 C
                 SUBROUTINE STUFF (ANGMOM, JJJ)
                  INTEGER RPM.XVALUE, YVALUE
                 DIMENSION WEIGH1 (122), WEIGH2 (122), WEIGH3 (122), WEIGH4 (122)
                 DIMENSION WEIGH6(122), WEIGH7(122), WEIGH8(122), WEIGH9(122)
                  DIMENSION WEIGHO(122), R(122), WEIGH5(122), R1(122)
                  DIMENSION IARRAY(10)
                  COMMON /WEIR/ WEIGHT, WEIGHZ, 
                *WEIGH7, WEIGH8, WEIGH9, WEIGHO, R
                  COMMON /URPI/ U,RP,PI
                  0.1 = NINX
                  XMAX = 10.0
                  O.O = MIMY
                  YMAX = 5.0
                  XVALUE= 9
                  YVALUE= 5
                  PRINT *,"DO YOU WANT WHEEL PLOT FOR:"
  20
                  PRINT *,"
PRINT *,"
PRINT *,"
                                                    1- HOOP"
                                                   2- SOLID CYLINDER"
                                                   3- ANNULAR CYLINDER"
                   READ *,M
                   IF (M.LT.1.OR.M.GT.3) 20,40
                   IF (M.EQ.3) 60,80
   40
                   PRINT *, "ENTER THICKNESS OF ANNULAR CYLINDER IN INCHES"
   60
                   READ * THICK
                   [=]
   80
                   ZNUM= (XMAX-XMIN)/100.
                   RADIUS= XMIN
```

```
IF (M.EQ.3) 100,140
100
      D0 120 J=2,102
      R(J) = RADIUS
      R1(J)= RADIUS+THICK
      RADIUS= RADIUS+ZNUM
120
      CONTINUE
      GOTO 180
      DO 160 J=2,102
140
      R(J) = RADIUS
      R1(J) = 0.0
      RADIUS= RADIUS+ZNUM
160
      CONTINUE
      ACC= U/RP**2
180
      IF (M.EQ.1) 200,220
200
      HUMACC= ANGMOM*ACC
      GOTO 240
220
      HUMACC= 2.*ANGMOM*ACC
      DO 480 RPM= 500,5000,500
240
      OMEGA= RPM/60.*2.*PI
      DO 460 J=2,102
      GOTO (260,280,300,320,340,360,380,400,420,440) I
      WEIGH1(J)= HUMACC/(OMEGA*(R(J)**2+R1(J)**2))
260
      GOTO 460
      WEIGH2(J) = HUMACC/(OMEGA*(R(J)**2+R1(J)**2))
280
      GOTO 460
      WEIGH3(J)= HUMACC/(OMEGA*(R(J)**2+R1(J)**2))
300
      GOTO 460
      WEIGH4(J)= HUMACC/(OMEGA*(R(J)**2+R1(J)**2))
320
      GOTO 460
      WEIGH5(J)= HUMACC/(OMEGA*(R(J)**2+R1(J)**2))
340
      GOTO 460
      WEIGH6(J)= HUMACC/(OMEGA*(R(J)**2+R1(J)**2))
360
      WEIGH7(J)= HUMACC/(OMEGA*(R(J)**2+R1(J)**2))
380
      GOTO 460
      WEIGH8(J)= HUMACC/(OMEGA*(R(J)**2+R1(J)**2))
400
       GOTO 460
      WEIGH9(J)= HUMACC/(OMEGA*(R(J)**2+R1(J)**2))
420
       GOTO 460
      WEIGHO(J)= HUMACC/(OMEGA*(R(J)**2+R1(J)**2))
440
460
       CONTINUE
       I = I + I
480
       CONTINUE
       CALL BINITT
490
       CALL SLIMY(155,730)
       CALL SLIMX(170,920)
       CALL XTICS (XVALUE)
       CALL YTICS (YVALUE)
       CALL XNEAT (0)
       CALL YNEAT (0)
```

```
CALL NEWPAG
      CALL NOTX (5,500,5,5HWHEEL)
      CALL NOTX(0,485,6,6HWEIGHT)
      CALL NOTX(8,470,4,4H(LB))
      CALL NOTX (440,60,17,17HWHEEL RADIUS (IN))
      CALL NOTX (370,0,36,36HRPM'S VARY FROM 500 TO 5000 STEP 500)
      GOTO (500,520,540) JJJ
      CALL NOTX (445,30,16,16HNON-GIMBLED PLOT)
500
       GOTO 560
520
      CALL NOTX (480,30,8,8HCMG PLOT)
      GOTO 560
      CALL NOTX (470,30,9,9HDMCD PLOT)
540
      GOTO (580,600,620) II
560
      CALL NOTX (490,15,4,4HH00P)
580
      GOTO 640
      CALL NOTX (450,15,14,14HSOLID CYLINDER)
600
      GOTO 640
      CALL NOTX (350,15,28,28HANNULAR CYLINDER: THICKNESS-)
620
      CALL NOTX (650, 15, 6, 6HINCHES)
      CALL FFORM (THICK, 5, 2, IARRAY, 32)
      CALL NOTAT (600,15,5,IARRAY)
      CALL DLIMX (XMIN, XMAX)
640
      CALL DLIMY (YMIN, YMAX)
      CALL CHECK (R, WEIGHT)
      CALL DSPLAY (R, WEIGHT)
      CALL CPLOT (R, WEIGH2) CALL CPLOT (R, WEIGH3)
      CALL CPLOT (R, WEIGH4)
      CALL CPLOT (R, WEIGH5)
      CALL CPLOT (R, WEIGH6)
CALL CPLOT (R, WEIGH7)
      CALL CPLOT (R, NEIGH8)
      CALL CPLOT (R, WEIGH9)
       CALL CPLOT (R.WEIGHO)
       CALL HOME
       CALL EPAUSE
       CALL CHANGE (XVALUE, YVALUE, XMIN, XMAX, YMIN, YMAX, JJ)
       IF (JJ.EQ.2) RETURN
       IF (JJ.EQ.3) GOTO 490
       GOTO 80
       END
          SUBROUTINE USED TO CHANGE NAUTICAL MILES TO FEET
       SUBROUTINE FEET (CHANGE)
       CHANGE= CHANGE*6076.103
       RETURN
       END
C
```

```
SUBROUTINE USED TO DISPLAY INPUTS
C
      SUBROUTINE REPLACE
      COMMON INPUT, LOC, REAL, EXP
      DIMENSION LOC(5), REAL(9), EXP(12), INPUT(277)
      PRINT 5000, INPUT(1), INPUT(2), INPUT(3),
20
     *INPUT(4), INPUT(5), LOC(1)
       D0 40 J=6,20,5
      PRINT 5015, INPUT(J), INPUT(J+1), INPUT(J+2),
     *INPUT(J+3), INPUT(J+4)
       CONTINUE
40
       PRINT 5005, INPUT(21), INPUT(22), INPUT(23),
      *INPUT(24), INPUT(25), LOC(2)
       D0\ 60\ J=26,40,5
       PRINT 5015, INPUT(J), IMPUT(J+1), IMPUT(J+2),
      *INPUT(J+3),INPUT(J+4)
       CONTINUE
 60
       PRINT 5010, INPUT(41), INPUT(42), INPUT(43),
      *INPUT(44),INPUT(45),LOC(3)
       PRINT 5020
 80
       READ *, CHECK
       PRINT 5035
       IF (CHECK.EQ.1) GOTO 120
        IF (CHECK.EQ.2) 100,80
        CALL ONE
 100
        PRINT 5035
        GOTO 20
 120
        II = 46
        DO 140 J=1,9
        PRINT 5025, J, INPUT(II), INPUT(II+1), INPUT(II+2),
       *INPUT(II+3), INPUT(II+4), REAL(J)
        II = II + 5
        CONTINUE
 140
        PRINT 5020
 160
        READ *, CHECK
        PRINT 5035
        IF (CHECK.EQ.1) GOTO 200
        IF (CHECK.EQ.2) 180,160
        CALL TWO
  180
        PRINT 5035
        GOTO 120
        II = 91
  200
        DO 220 J=1,12
        PRINT 5030, J, INPUT(II), INPUT(II+1), INPUT(II+2),
        *INPUT(II+3), INPUT(II+4), INPUT(II+5), EXP(J)
         II = II + 6
         CONTINUE
  220
         PRINT 5020
  240
         READ *, CHECK
         PRINT 5035
```

```
IF (CHECK.EQ.1) GOTO 280
       IF (CHECK.EQ.2) 260,240
260
       CALL THREE
       PRINT 5035
       GOTO 200
       RETURN
280
5000 FORMAT (1X,"1",1X,4A10,A5,I3)
5005 FORMAT (1X,"2",1X,4A10,A5,I3)
5010 FORMAT (1X,"3",1X,4A10,A5,I3)
5015 FORMAT (3X,4A10,A5)
5020 FORMAT (///,1X,"IF INPUTS OK ENTER 1",/,1X,"IF WANT TO CHANGE",
*" ENTER 2")
5025 FORMAT (I2,1X,5A10,F10.3)
     FORMAT (12,1X,6A10,E10.4)
5030
5035 FORMAT (//)
       END
C
          SUBROUTINE USED TO CHANGE INTEGER INPUTS
C
C
       SUBROUTINE ONE
       COMMON INPUT, LOC, REAL, EXP
       DIMENSION LOC(5), REAL(9), EXP(12), INPUT(277)
       PRINT *, "ENTER NUMBER, NEW VALUE (INTEGER)"
20
       PRINT *,"ENTER 0,0 TO STOP"
READ *, NUM, IVALUE
40
       IF (NUM.EQ.O) RETURN
       IF ((NUM.EQ.1.OR.NUM.EQ.2).AND.(IVALUE.LT.1.OR.IVALUE.GT.3))
      *G0T0 20
       IF (NUM.LT.1.OR.NUM.GT.3) GOTO 20
       LOC(NUM) = IVALUE
       GOTO 40
       RETURN
       END
C
           SUBROUTINE USED TO CHANGE REAL INPUTS
C
C
       SUBROUTINE TWO
       COMMON INPUT, LOC, REAL, EXP
       DIMENSION LOC(5), REAL(9), EXP(12), INPUT(277)
       PRINT *, "ENTER NUMBER, NEW VALUE (REAL)"
PRINT *, "ENTER 0,0. TO STOP"
20
40
        READ *, NUM, VALUE
        IF (NUM.EQ.O) RETURN
        IF (NUM.LT.1.OR.NUM.GT.9) GOTO 20
        REAL(NUM) = VALUE
        GOTO 40
        RETURN
        END
 C
```

```
C SUBROUTINE USED TO CHANGE EXP. INPUTS

C SUBROUTINE THREE COMMON INPUT,LOC,REAL,EXP
DIMENSION LOC(5),REAL(9),EXP(12),INPUT(277)

20 PRINT *,"ENTER NUMBER, NEW VALUE (EXP)"
PRINT *,"ENTER 0,0. TO STOP"

40 READ *,NUM,VALUE
IF (NUM.EQ.0) RETURN
IF (NUM.LT.1.OR.NUM.GT.12) GOTO 20

EXP(NUM) = VALUE
GOTO 40
RETURN
END

/
```

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TABLE I. CONVERSION FACTORS FROM U.S. CUSTOMARY TO S.I. UNITS

,		
1 inch	= .	2.54 centimeters
1 foot	=	0.305 meters
1 mile	=	1.61 kilometers
1 pound (wt)	=	4.95 newtons = 0.454 kilograms
1 foot-pound	=	1.38 newton-meters
1 slug-foot ²	= '	1.36 kilogram-meters ²
1 slug-foot ² seconds	=	1.36 <u>kilogram-meters</u> seconds

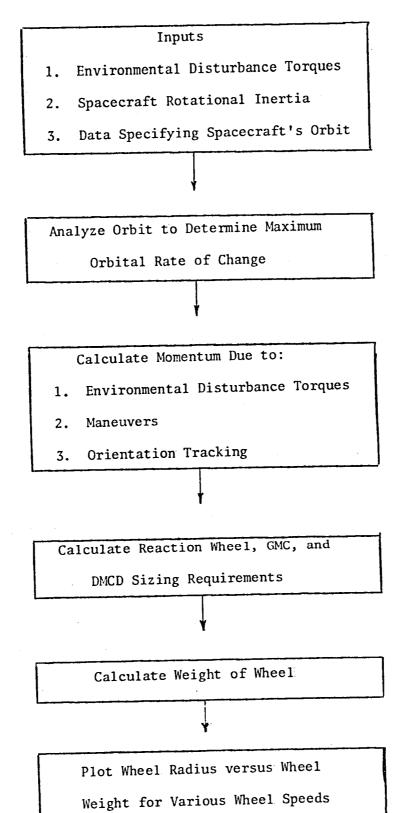


Figure 1. Flow diagram.

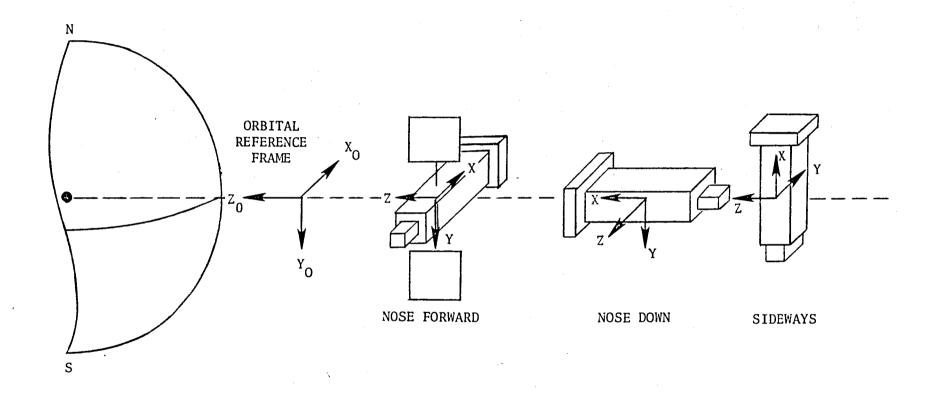


Figure 2. Relationship between the orbital reference frame and the three vehicle reference frames.

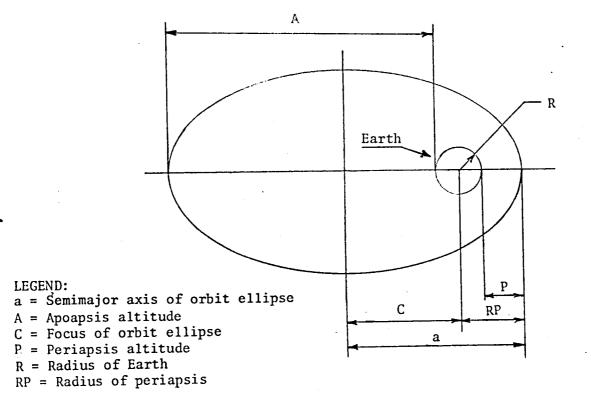


Figure 3. Orbit definition.

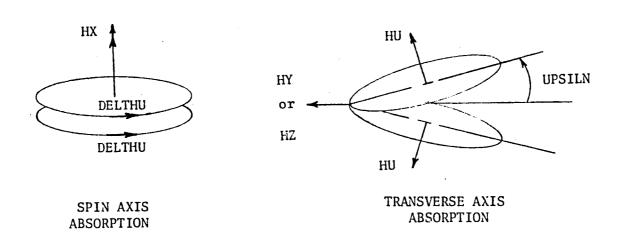
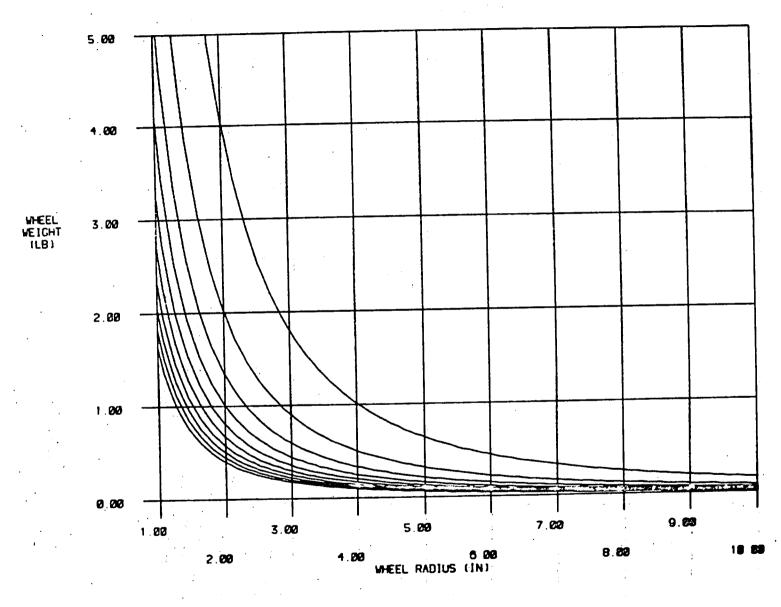


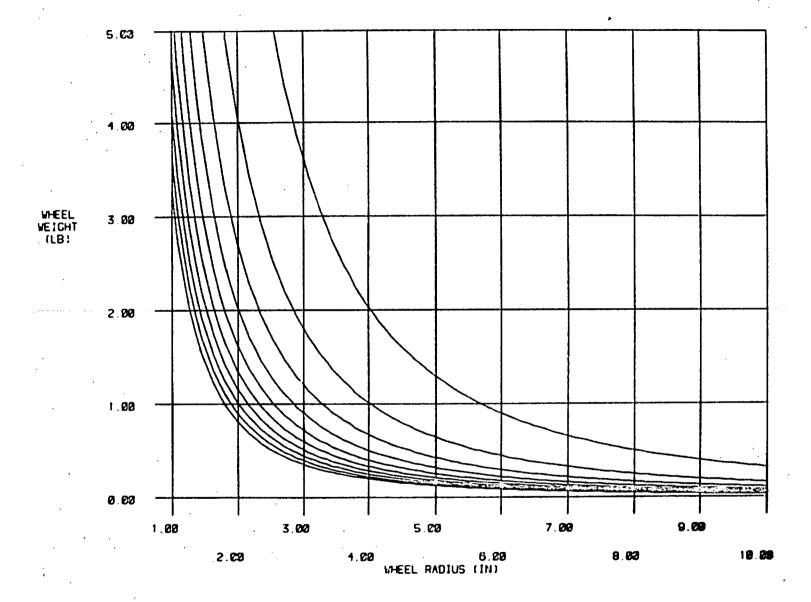
Figure 4. DMCD configuration.



RPH'S VARY FROM SES TO SEES STEP 500

(a) Hoop.

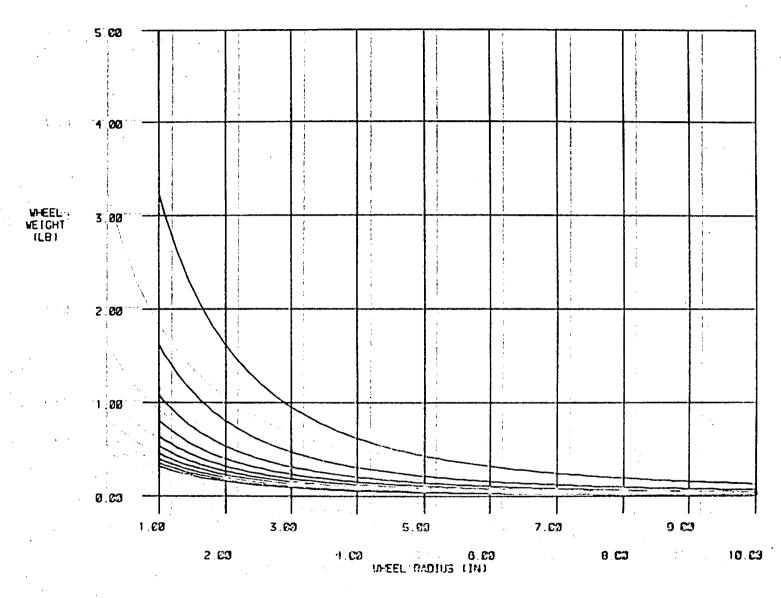
Figure 5. Weight curves for nongimbled reaction wheel.



RPH'S VARY FROM SCO TO SCCO STEP SCO

(b) Solid cylinder.

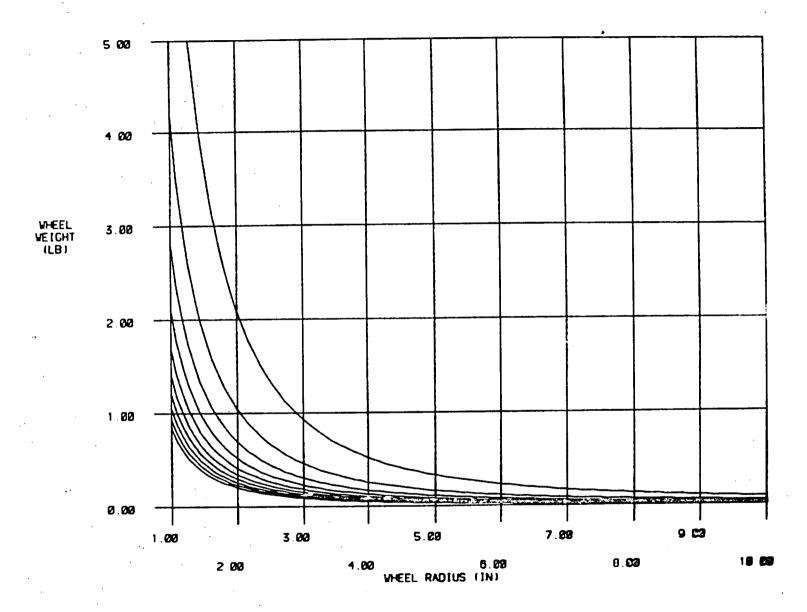
Figure 5. Continued.



MODULAR CYLINDER: THICKNESS- 2 CD INCHES

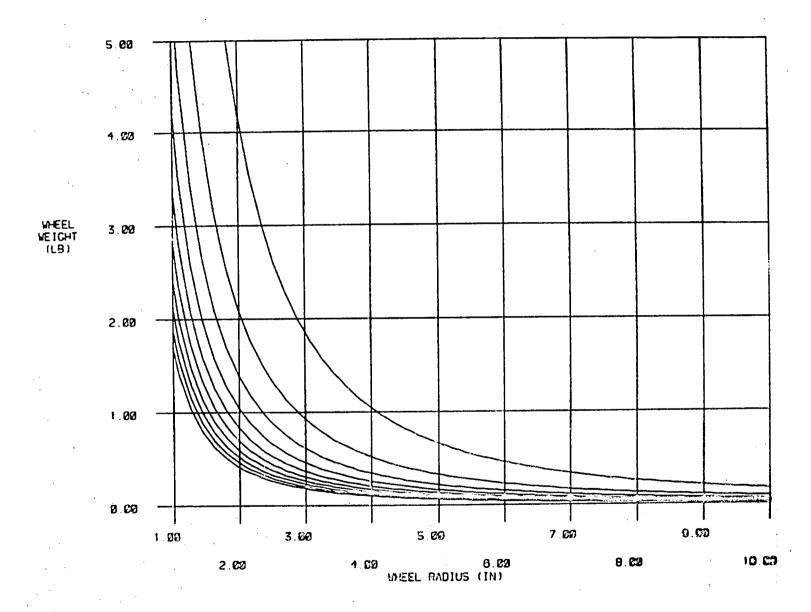
(c) Annular cylinder.

Figure 5. Concluded.



RPM'S VARY FROM EACH TO EACH STEP ESS (a) Hoop.

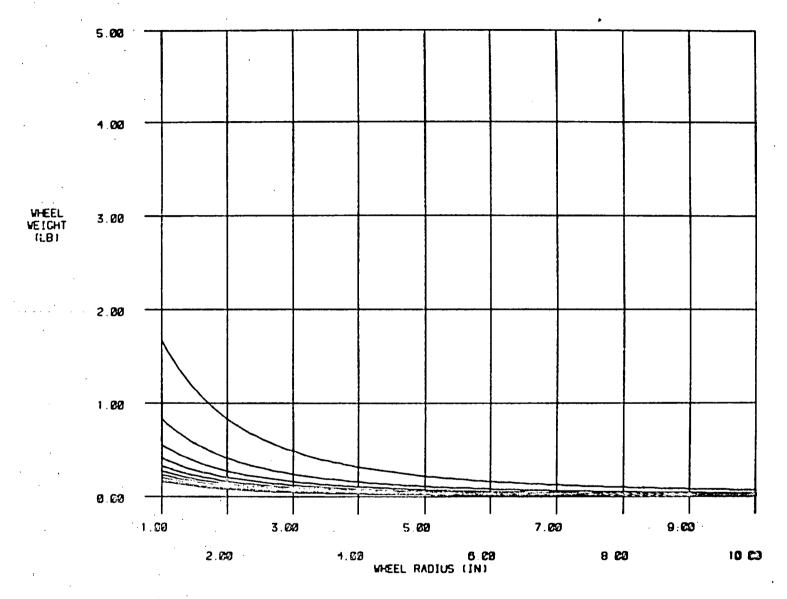
Figure 6. Weight curve for CMG.



RPH'S VARY FROM SOU TO SOOD STEP SOO

(b) Solid cylinder.

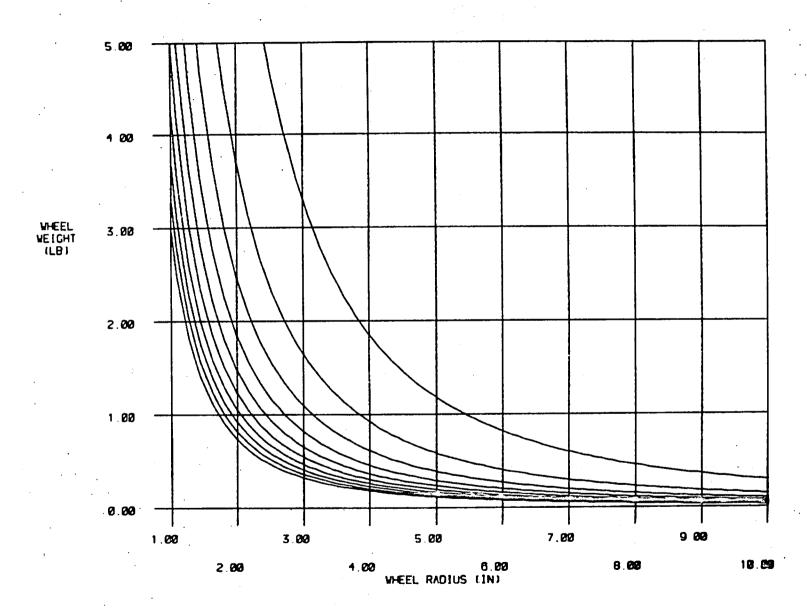
Figure 6. Continued.



ANNULAR CYLINGER: THICKNESS- 2 CO INDRES

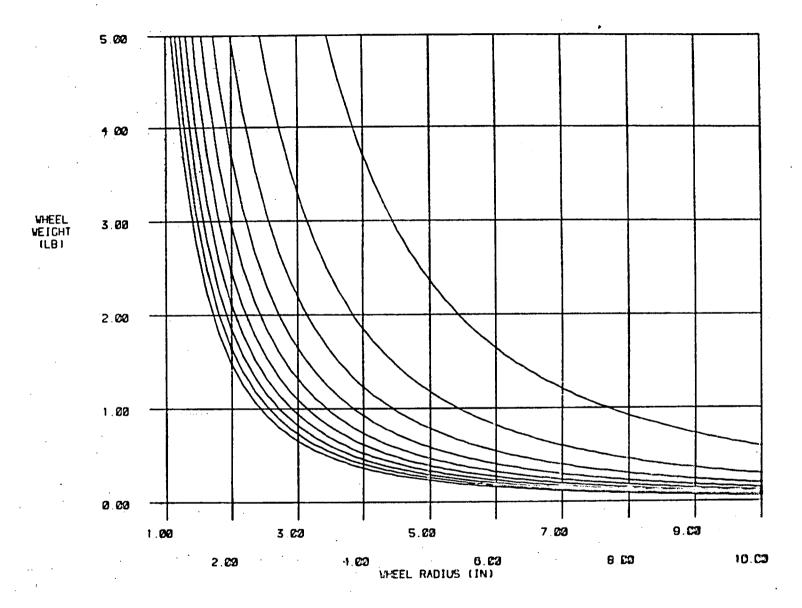
(c) Annular cylinder.

Figure 6. Concluded.



RPM'S VARY FROM 500 TO 5000 STEP 520 (a) Hoop.

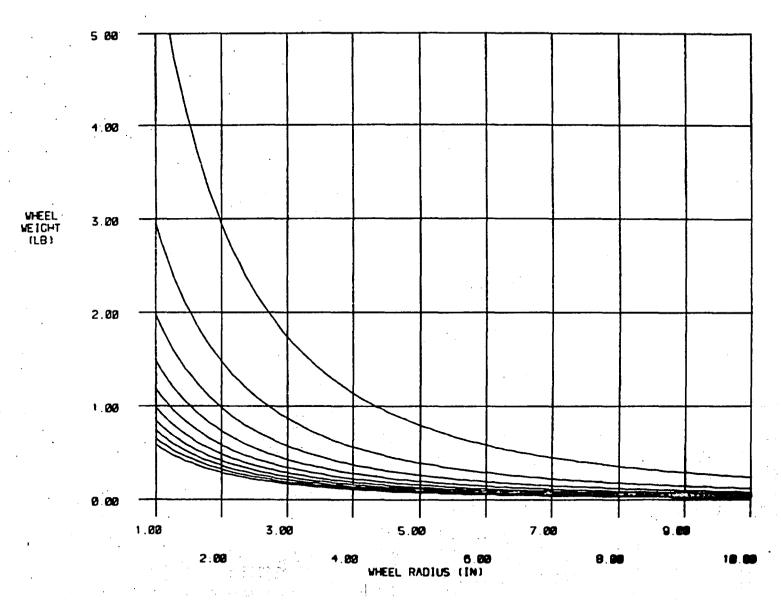
Figure 7. Weight curves for DMCD.



RPH'S VARY FROM 500 TO 5000 STEP 500

(b) Solid cylinder.

Figure 7. Continued.



ANNULAR CYLINDER: THICHESS- 2.89 INCHES RPM'S VARY FROM 568 TO 5868 STEP 588

(c) Annular cylinder.

Figure 7. Concluded.

```
VEHICLE POINTING ORIENTATION
                                                 3
1 INOSE-
           1= SIDEWAYS
           2= NOSE DOVIN
           3= NOSE FORWARD
                                                 1
          CELESTIAL ORIENTATION
2 ISATOR-
           1= EARTH
           2= SUN
           3= INERTIAL
           NUMBER OF GIMBALED CONFIGURATIONS
3 XNNN-
IF INPUTS OK ENTER 1
IF WANT TO CHANGE ENTER 2
           LENGTH OF APOAPSIS (ML)
1 APOA-
           LENGTH OF PERIAPSIS (IIL)
2 PER-
3 ORBINC- ORBIT INCLINATION (DEG)
           TIME BETWEEN WHEEL UNLOADING (ORBITS)
4 TL-
5 TACCEL- MANEUVER ACCELERATION TIME (SEC)
```

IF INPUTS OK ENTER 1 IF WANT TO CHANGE ENTER 2

6 PDOTRX- X-AXIS MANEUVER RATE (DEG/SEC)
7 PDOTRY- Y-AXIS MANEUVER RATE (DEG/SEC)

8 PDOTRZ- Z-AXIS MANEUVER RATE (DEG/SEC)

9 UPSILN- ANGULAR PIVOTING FOR DMCD (DEG)

1 TAX- 2 TGX- 3 TSX- 4 TAY- 5 TGY- 6 TSY- 7 TAZ-	X-AXIS ATMOSPHERIC DIST. TORQUE (FT-LBS) X-AXIS GRAVITY GRAD. DIST. TORQUE (FT-LBS) X-AXIS SOLAR DIST. TORQUE (FT-LBS) Y-AXIS ATMOSPHERIC DIST. TORQUE (FT-LBS) Y-AXIS GRAVITY GRAD. DIST. TORQUE (FT-LBS) Y-AXIS SOLAR DIST. TORQUE (FT-LBS) Z-AXIS ATMOSPHERIC DIST. TORQUE (FT-LBS)	0. .2859E-10 0. .8541E-06 .3791E-10 0. .8477E-07
8 TGZ-	Z-AXIS GRAVITY GRAD. DIST. TORQUE (FT-LBS)	0.
9 TSZ-	Z-AXIS SOLAR DIST. TORQUE (FT-LBS)	0.
10 XJ-	X-AXIS SPACECRAFT ROTATIONAL INERTIA (SLUG-FT**2)	.1595E+04
11 YJ-	Y-AXIS SPACECRAFT ROTATIONAL INERTIA (SLUG-FT**2)	.1380E+04
12 ZJ-	Z-AXIS SPACECRAFT ROTATIONAL INERTIA (SLUG-FT**2)	•8034E÷03

175.000

100.000

57.300

1.000

20,000

1.000 1.000

1.000

20.000

IF INPUTS OK ENTER 1
IF WANT TO CHANGE ENTER 2

Figure 8. Input default values.

APOA- RP- THETAD- T-	APOAPSIS ALTITUDE (FT) RADIUS AT PERIAPSIS (FT) MAXIMUM ORBITAL ANGULAR RATE (RAD/SEC) ORBITAL PERIOD (SEC)	.1063318E+07 .2151949E+08 .1194795E-02 .5370454E+04
ALL	MOMENTUM IN (SLUG-FT**2)/SEC	
HXMAN- HYMAN- HZMAN-		.2783595E+02 .2408377E+02 .1402094E+02
HTX- HTY- HTZ-	X-AXIS DISTURBANCE TORQUE MOMENTUM Y-AXIS DISTURBANCE TORQUE MOMENTUM Z-AXIS DISTURBANCE TORQUE MOMENTUM	.1535413E-06 .4587108E-02 .4552533E-03
HTRAKX- HTRAKY- HTRAKZ-	X-AXIS ORIENTATION TRACKING MOMENTUM Y-AXIS ORIENTATION TRACKING MOMENTUM Z-AXIS ORIENTATION TRACKING MOMENTUM	0. .1648818E+01 0.
HX- HY- HZ-	TOTAL X-AXIS MOMENTUM TOTAL Y-AXIS MOMENTUM TOTAL Z-AXIS MOMENTUM	.2783595E+02 .2573717E+02 .1402140E+02
HMAX- TMAX- HCMG-	MAXIMUM MOMENTUM ANY AXIS MAXIMUM TORQUE ANY AXIS (FT-LBS) CMG WHEEL MOMENTUM	.2783595E+02 .1391798E+01 .1435261E+02
DELDOT- TCMG- HTDMCD-	PEAK GIMBAL RATE (RAD/SEC) PEAK TORQUER TORQUE (FT-LBS) DMCD WHEEL MOMENTUM REQUIR.	.4112024E+02 .2504819E+00 .5078648E+02

Figure 9. Calculated output values.

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15. Supplementary Notes				
*Cooperative education st	udent at Georgia	Institute	e of Technolog	зу
16. Abstract				
dual momentum control de program accepts as input rotational inertias, man weights are calculated f the momentum wheel may he cylinder. The program protential between the we mediate calculations such absorption requirements analysis information are	ts the spacecraft's euver rates, and for a range of rade chosen to be eight, radius, and the x-, y-, for reaction whee	s environ orbital of the a houtput il wheel so and Z-axels, CMG'	nmental disturdata. From the otational specioop, solid cyllustrating the peed. A number is total moments, DMCD's, and	rbance torques, nese inputs, wheel eds. The shape of linder, or annular e trade-off er of the inter- ntum, the momentum
17 Vov. Words (Connected by Arabada)		18 Dictributi	on Statement	
17. Key Words (Suggested by Author(s))				imited
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-			Sı	abject Category 61,18
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